


## Exploited Populations

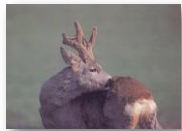
Population Modeling  
University of Florida  
Gainesville, FL  
February-March 2016

WATERFOWL HARVEST WATERFOWL DEMOGRAPHY HARVEST MANAGEMENT CONCLUSION

### Waterfowl harvest: nothing new



*Tomb of Khnumhotep, Dynasty 12, ca. 1897–1878 B.C., Beni Hasan, Egypt*



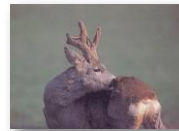
### Harvest and $\lambda$ Survival

$$M \rightarrow M_h = (1-h)M \quad MV = \lambda V \Rightarrow (1-h)MV = (1-h)\lambda V$$

Hence  $M_h V = (1-h)\lambda V$

$\lambda \rightarrow \lambda_h = (1-h)\lambda$ , asymptotic structure  $V$  unchanged

$x\%$  change in all  $s_i \rightarrow x\%$  change in  $\lambda$



### Harvest and $\lambda$ Survival

$$M \rightarrow M_h = (1-h)M \quad MV = \lambda V \Rightarrow (1-h)MV = (1-h)\lambda V$$

Hence  $M_h V = (1-h)\lambda V$

$\lambda \rightarrow \lambda_h = (1-h)\lambda$ , asymptotic

$s_i \rightarrow s_i(1-h)$   
if harvest or incidental mortality  
entirely before or after natural mortality.  
Then  $\lambda \rightarrow \lambda(1-h)$

$x\%$  change in all  $s_i \rightarrow x\%$  change in  $\lambda$

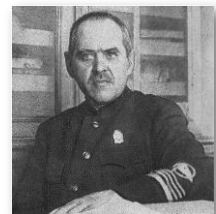
## Modeling Harvest Mortality

- Not quite as simple as appears on first glance

## Some History

Fedor Il'yich BARANOV,  
An officer of the Russian fleet,  
and a pioneer of the  
theory of exploited populations.

W.E. RICKER taught himself  
Russian to be able to read  
BARANOV's works.



### Exploitation in continuous time: mortality and exploitation as competing risks (Baranov, 1918)

"natural" dynamics of death :  $n(t+dt) - n(t) = -m n(t) dt$   
 with exploitation :  $n(t+dt) - n(t) = -(m+h) n(t) dt$   
 $m, h$ : natural mortality and harvest *instantaneous rates*  
 two sources of mortality assumed additive, with total rate  $z = m+h$   
 However, the number of individuals at risk for both sources of mortality varies with total mortality  $z$  as  $n(t) = n(0) \exp(-z t)$

### Exploitation in continuous time: mortality and exploitation as competing risks over $[0, T]$

Number of natural deaths  $\int_0^T n(t) m dt = m/z n(0)(1-e^{-zT})$   
 Number of deaths from exploitation  $= h/z n(0)(1-e^{-zT})$   
 Proportion of deaths from exploitation  $H = h/z (1-e^{-zT})$   
 Overall proportion of survivors  $S = e^{-zT}$   
 Proportion of survivors if no exploitation  $S_0 = e^{-mT}$

$\Rightarrow$  a complex relationship between  $S$ ,  $H$ , and  $S_0$  :

$$1 - H/(1 - S) = \log(S_0) / \log(S)$$

...  $S$  cannot be worked out as a simple function of  $H$  and  $S_0$

### Additive Risks: Instantaneous and Finite Rates

$S_0 = e^{-mT}$  = Probability that animal alive at time 0 survives nonhunting mortality sources until time  $T$  in the absence of any other mortality source

$1 - K = e^{-hT}$  = Probability that animal alive at time 0 survives hunting mortality sources until time  $T$  in the absence of any other mortality source

$S = S_0(1 - K) = e^{-(m+h)T}$  = Probability that animal alive at time 0 survives all mortality sources until time  $T$

### Additive Risks: Instantaneous and Finite Rates

$S = S_0(1 - K) = e^{-(m+h)T}$  = Probability that animal alive at time 0 survives all mortality sources until time  $T$

$S_0$  and  $K$  are referred to as finite "net rates", in the sense that they are applicable when no other mortality sources are operative

### Additive Risks: Instantaneous and Finite Rates

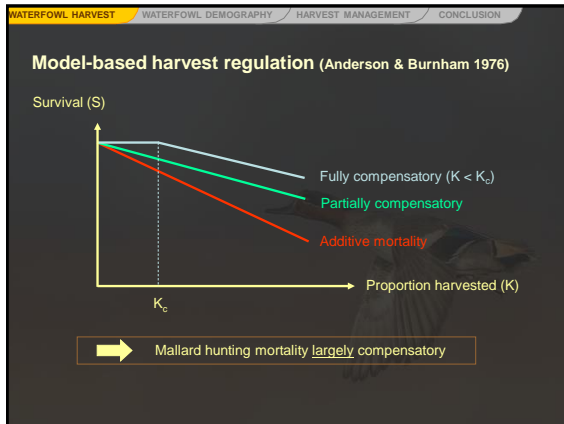
•  $S = S_0(1 - K) = e^{-(m+h)T}$  = Probability that animal alive at time 0 survives all mortality sources until time  $T$

• This expression holds true when the mortality sources are separated in time, e.g., hunting for  $(0, T)$  and nonhunting for  $(T, T)$

• The above expression also holds when there is no temporal separation of the mortality sources (both sources operate throughout  $(0, T)$ )

### N. A. Waterfowl Harvest Management

- 1960s-1970s: debate over whether harvest mortality really acted as an additive competing risk
- Alternative idea was that number of birds harvested had little to do with breeding population available in spring
  - If harvest mortality increased then nonhunting mortality decreased



## Investigating Effects of Harvest

- Lots of poor inference procedures used to support different views, e.g.,
- Proponents of additive mortality hypothesis would frequently plot estimated harvest and annual survival rates for different locations
- Always obtained linear negative relationship, but it resulted from a negative sampling covariance  $\text{cov}(\hat{h}_j, \hat{S}_j)$

## Investigating Effects of Harvest

- Proponents of compensatory mortality hypothesis often confuse net and crude rates
  - Crude mortality rate is the proportion of individuals that die of focal mortality source in the presence of other sources
  - Denote crude rate with prime, e.g.,  $S'_0$
- But crude rates depend on the magnitude of other operative rates and are hence tricky to interpret

## Investigating Effects of Harvest

- Year divided into hunt season followed by no-hunt season, so  $S = S_0(1 - K)$
- Hunting occurs first, so  $K = K'$ , but
 
$$1 - S'_0 = (1 - K)(1 - S_0)$$
- Example:
  - $S_0 = 0.8$ ,  $K = 0.05$ ,  $1 - S'_0 = 0.19$
  - $S_0 = 0.8$ ,  $K = 0.15$ ,  $1 - S'_0 = 0.17$
- Inverse relationship between  $K$  and  $1 - S'_0$  might appear to support compensatory hypothesis, but the example shows additive mortality

## Investigating Effects of Harvest: N.A. Mallards, 1987-2015

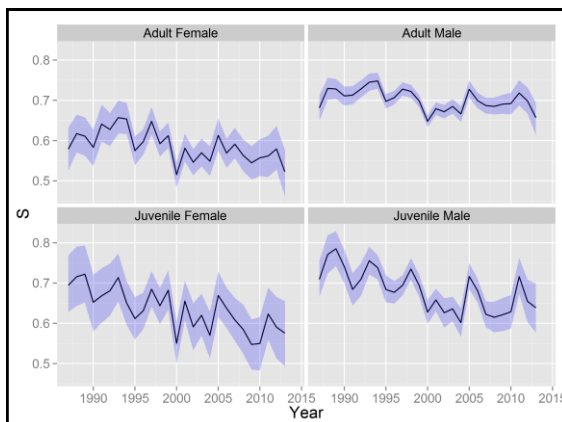
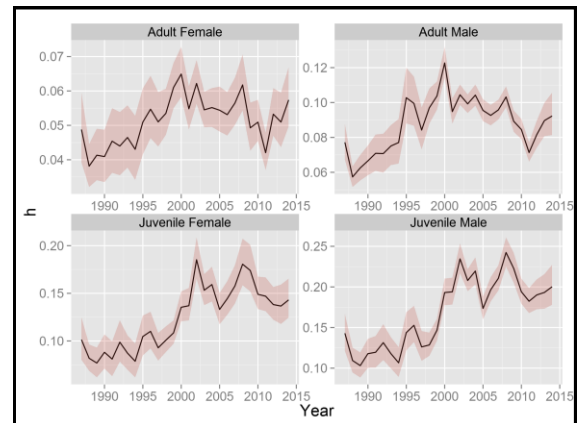
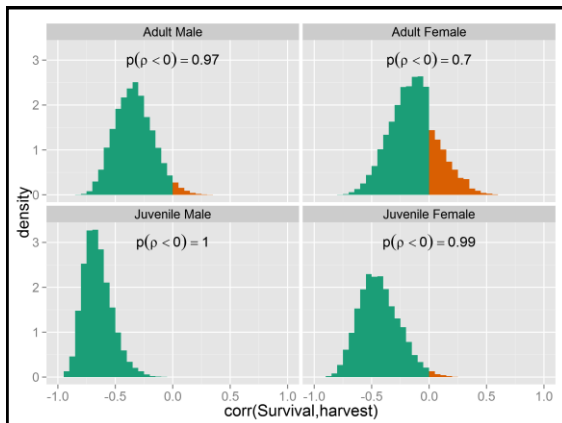
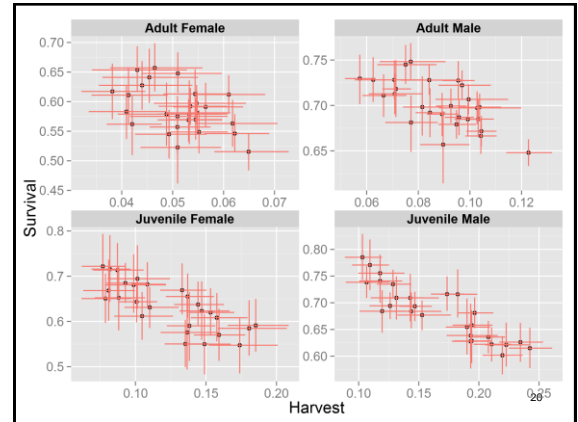
- Effects of hunting question important to management
- Boomer et al. (in review) recently undertook a thorough analysis of mallard survival and harvest rates

## Harvest and Survival Estimation for N.A. Mallards

- Band reporting probabilities can vary over time and space:
  - Band inscription
  - Reporting methods
  - Recovery areas
  - Hunter behavior
- What is the relationship between harvest and survival over a time period with differing harvest regulations?

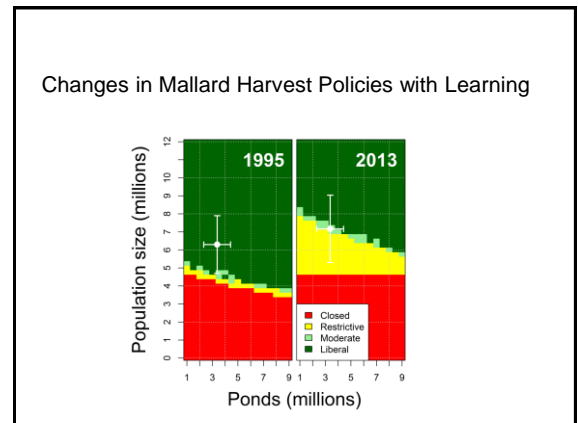
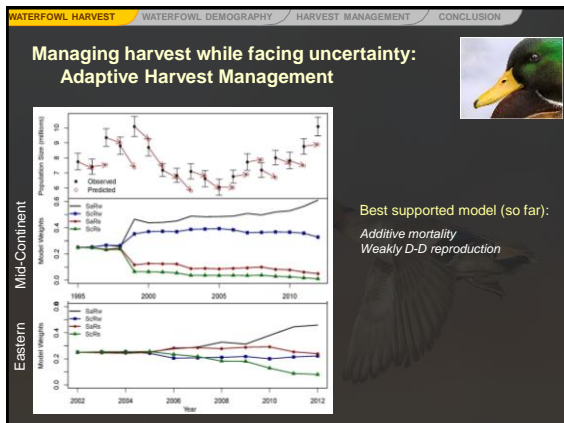
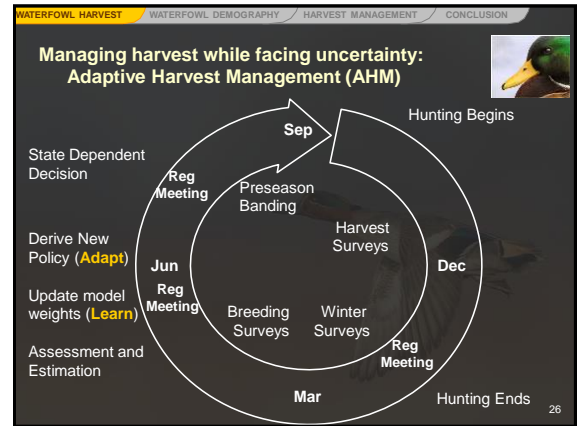
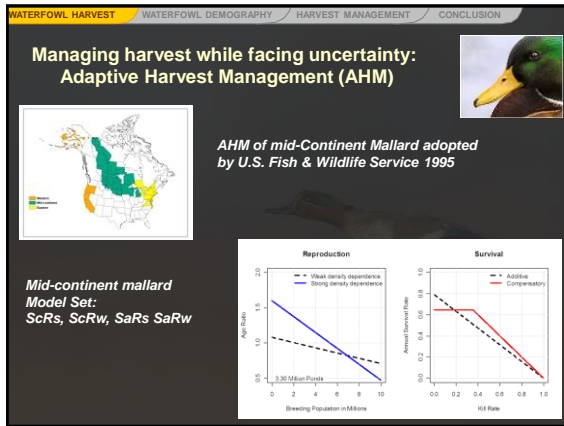
## Limited Range of Harvest Rates Since 1995

- Used data from 1987 for analysis
- Included more variation in harvest rates, e.g.,
  - Adult males:  $0.05 < h < 0.13$
  - Young males:  $0.10 < h < 0.25$



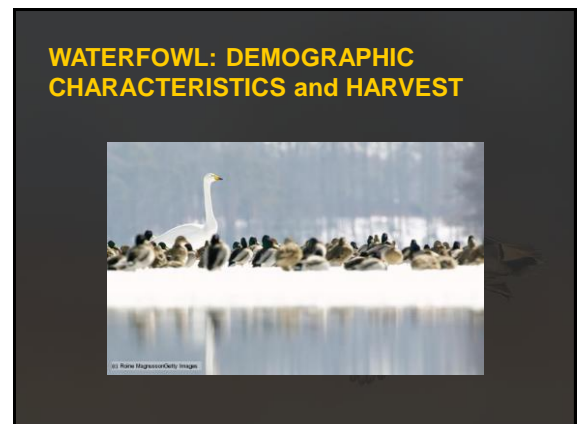
## Harvest Management for N.A. Mallards

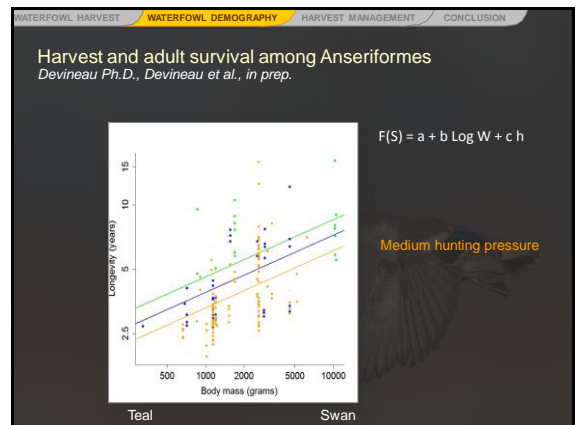
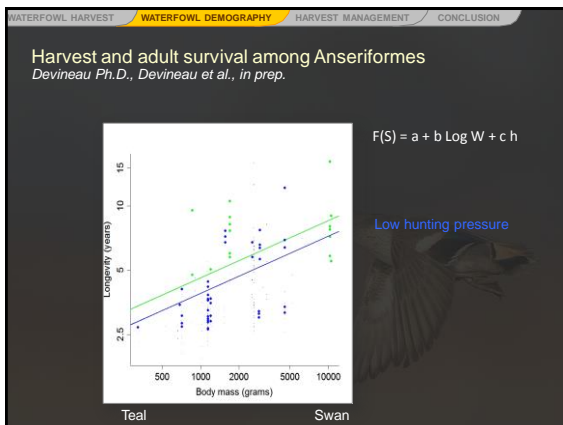
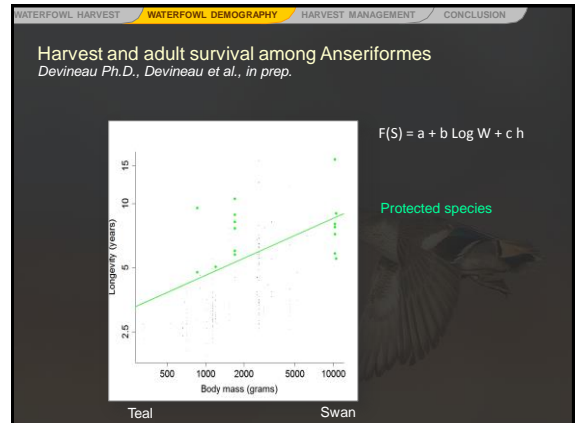
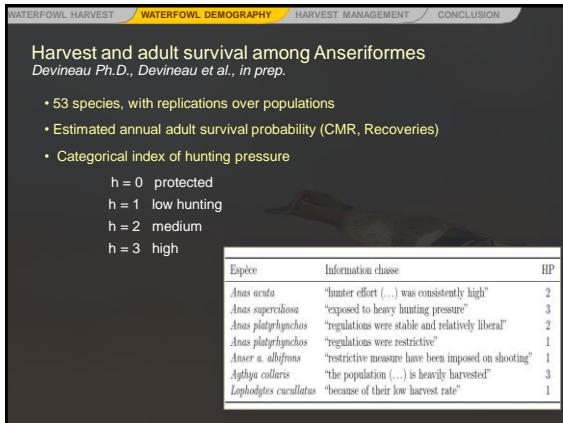
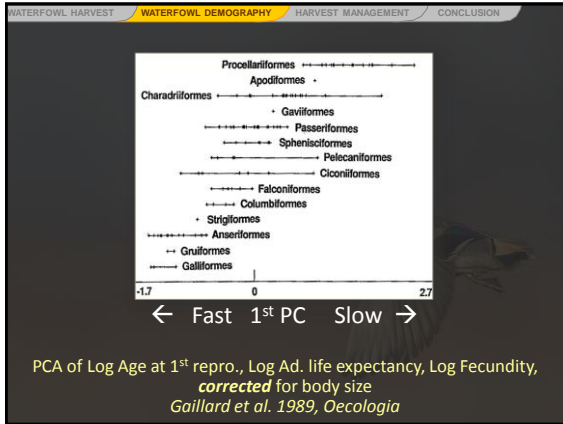
- So we now have fairly strong evidence of substantial additivity of hunting mortality
- But this analysis is new, and what about reproductive effects?
- How have we been managing mallards in the face of this uncertainty?

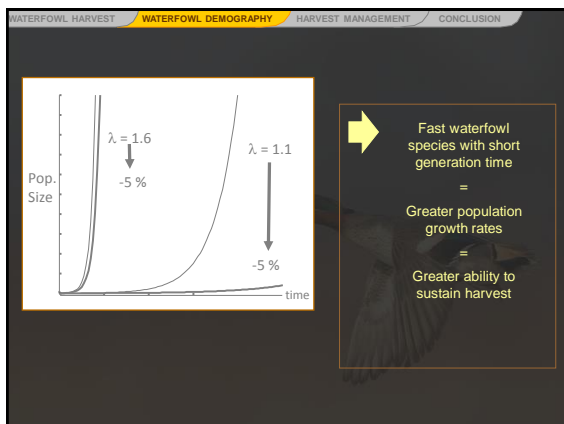
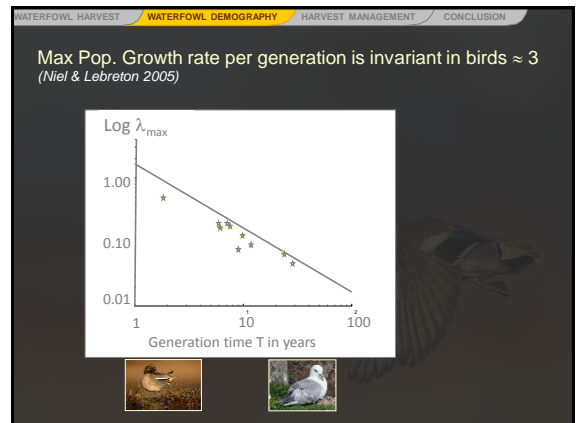
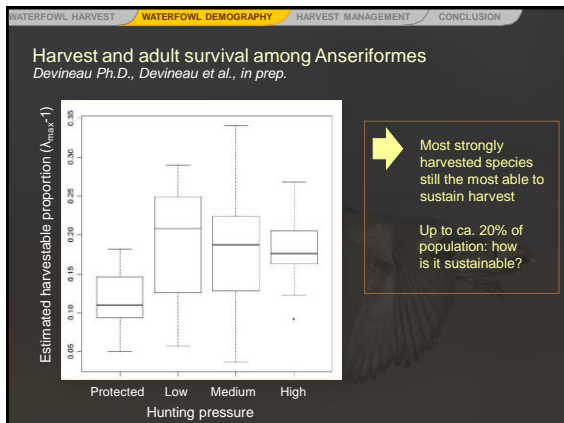
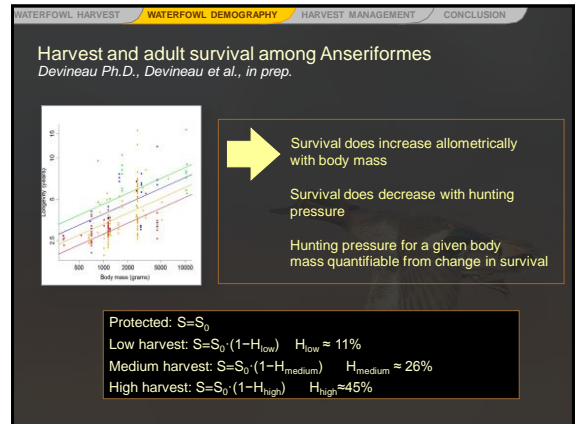
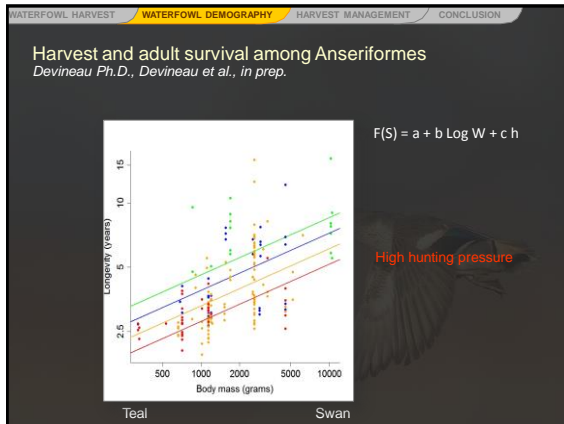


## Adaptive Management Mid-Continent Mallards

- Provided a natural way to manage in the face of uncertainty
- Permitted us to learn
  - Increased “weight” on additive model is consistent with recent survival analyses
- Permitted us to use what has been learned as we proceeded







## Compensatory Mechanisms

- Original compensatory mortality hypothesis is phenomenological:

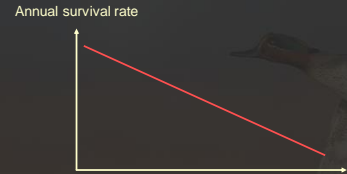

$$S = S_0(1 - bK); b \rightarrow 0 \mid K < C$$

- When it does seem to fit data, what sorts of mechanisms might be responsible?
  - Density-dependence
  - Heterogeneity

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / **HARVEST MANAGEMENT** / CONCLUSION

### Compensation by density-dependence

Non-harvest mortality or fecundity decreases with density of individuals so that reduction in population size due to harvest leads to fitness improvement of harvest survivors.

Some evidence for DD non-hunting mortality in waterfowl (e.g. Ring-necked duck in Conroy & Eberhardt 1983)

## How Might We Model Density-Dependent Survival?

- Johnson et al. (1993) proposed

$$S_t = S_{0,t}(1 - K_t)$$

$$S_{0,t} = \frac{e^{\beta_0 + \beta_1 N_t(1 - K_t)}}{1 + e^{\beta_0 + \beta_1 N_t(1 - K_t)}}$$

- So post-hunting season survival is modeled as a function of post-season density
  - Expectation that  $\beta_1 < 0$

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / **HARVEST MANAGEMENT** / CONCLUSION

### Compensation by density-dependence of survival

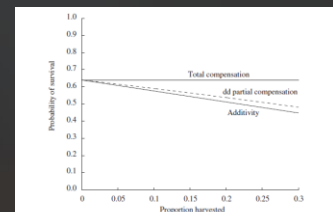



Figure 3. An example of compensation by density-dependence. Survival at density  $N$  is 0.64. Density-dependence is strong enough to make survival probability decrease to 0.48 (a 25% decrease) if population size doubles. Despite this strong density-dependence, compensation of harvest is weak, the dotted line being close to  $S_0(1 - 0.825K)$ . (Lebreton (2005))

➡ Compensation by DD survival is weak at best

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / **HARVEST MANAGEMENT** / CONCLUSION

### Compensation by density-dependence of fecundity



Survival of semi-natural Mallard nests does decrease with increasing nest density (Elmberg et al. 2009)  
Similar evidence for N.A. prairies (Dzubin 1969)

Recruitment can compensate harvest if  $\frac{\Delta F}{F} \approx TK$  (Lebreton 2005)

➡ Dabbling ducks with a 1.5 years generation time would need a 15% increase in  $F$  to compensate a 10% harvest: is this realistic?

Would so many 1st year females attempt breeding without hunting?

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / **HARVEST MANAGEMENT** / CONCLUSION


### Compensation by heterogeneity

**Scalar models: all individuals equivalent**

Unharvested:  $N_{t+1} = \lambda N_t$

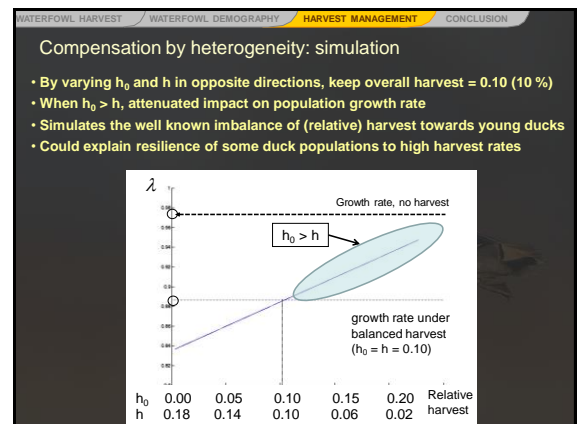
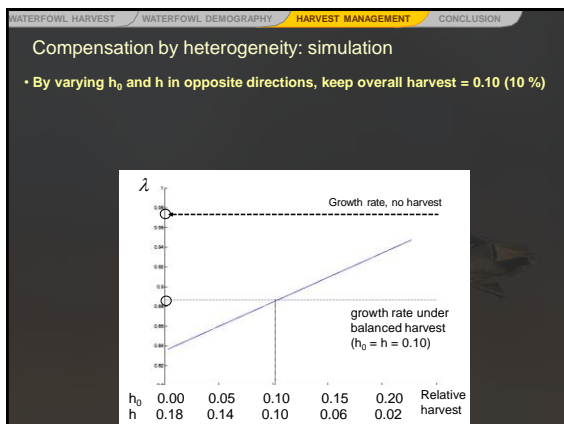
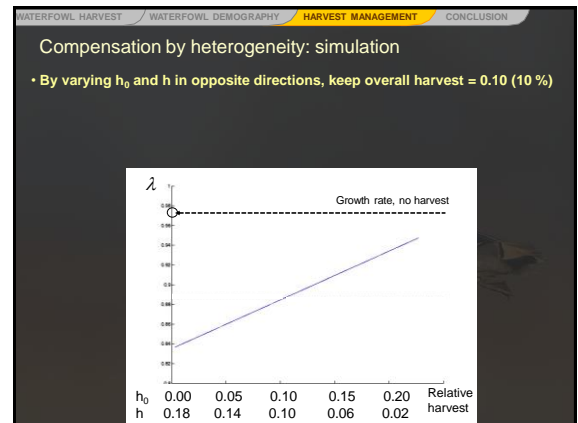
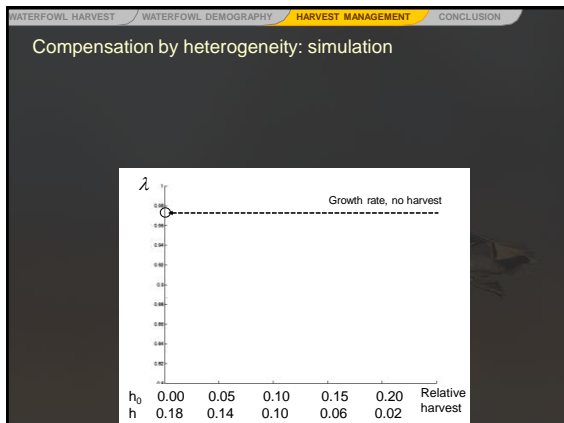
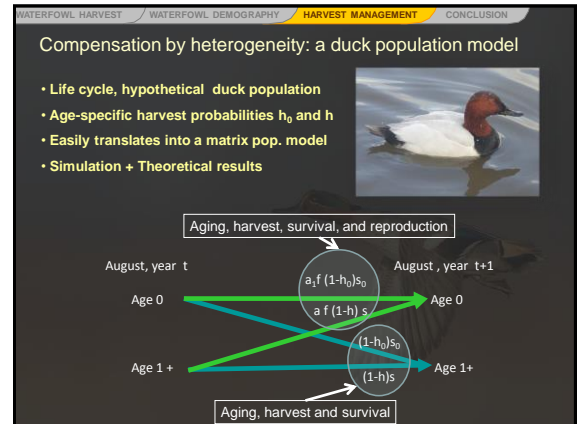
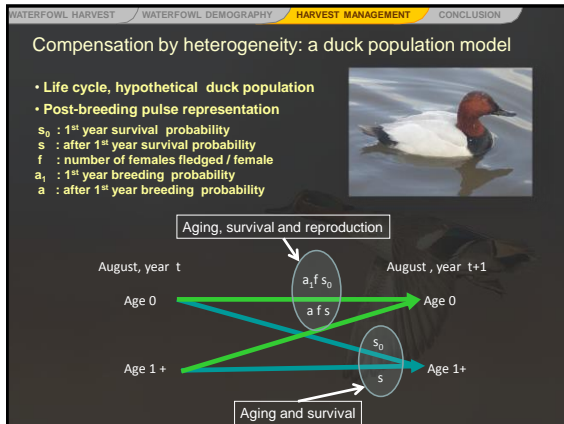
Proportional harvest:  $N_{t+1} = (1 - h)\lambda N_t$

**This is not the real world ! Populations are heterogeneous, i.e. structured ! (Johnson et al. 1986)**



inside vs outside





WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / HARVEST MANAGEMENT / CONCLUSION

### Compensation by heterogeneity: Theoretical results

- Changes in  $h_0$  and  $h$  are changes in overall survival  $s_0(1-h_0)$  and  $s(1-h)$
- Effect on growth rate  $\lambda$  depends on elasticities (« relative sensitivities »)
- Sensitivities can be expressed as a function of generation time  $T = 5.5167$  y

Age class	0	1+
Stable asymptotic structure	$W_0 = 0.4521$	$W_1 = 0.5479$
Reproductive value (=contribution to growth)	$V_0 = 0.4009$	$V_1 = 1.4943$
Elasticity		
$\frac{\partial \log \lambda}{\partial \log s_0}$	$1/T = V_0 W_0 = 0.1813$	
$\frac{\partial \log \lambda}{\partial \log s_1}$		$1-1/T = V_1 W_1 = 0.8187$

## Compensation by Heterogeneity

- Estimation and modeling are much easier when heterogeneity is associated with an identifiable characteristic such as age
- What about individual frailty?
  - Vital rate variation among individuals not associated with any identifiable characteristic (can't tell quality of bird in hand)

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / HARVEST MANAGEMENT / CONCLUSION

### Compensation by heterogeneity: Individual Frailty

Lindberg, Lebreton, Boomer, unpublished




- Canvasback *Aythya valisineria*
- 2 classes of “demographic quality” (purely phenotypical)  
POOR and GOOD
- A discrete mixture model for a continuous heterogeneity
- “POOR” individuals more vulnerable to hunting than “GOOD”

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / HARVEST MANAGEMENT / CONCLUSION

### Compensation by heterogeneity: Individual Frailty

Lindberg, Lebreton, Boomer, unpublished


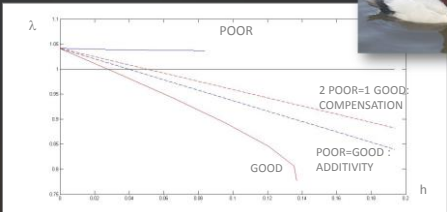


AGE	1	1	2+	2+
QUALITY	POOR	GOOD	POOR	GOOD
AGE QUALITY				
1 POOR	0	$a_{1p} * f_{gp} * S_{1p} * (1-h_p)$	$a_p * f_{pp} * S_{1p} * (1-h_p)$	$a_b * f_{gp} * S_{1p} * (1-h_p)$
1 GOOD	0	$a_{1g} * f_{gg} * S_{1g} * (1-h_g)$	$a_p * f_{pg} * S_{1g} * (1-h_g)$	$a_b * f_{gg} * S_{1g} * (1-h_g)$
2+ POOR	$S_p * (1-h_p)$	0	$S_p * (1-h_p)$	0
2+ GOOD	0	$S_g * (1-h_g)$	0	$S_g * (1-h_g)$

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / HARVEST MANAGEMENT / CONCLUSION

### Compensation by heterogeneity: Individual Frailty

Lindberg, Lebreton, Boomer, unpublished


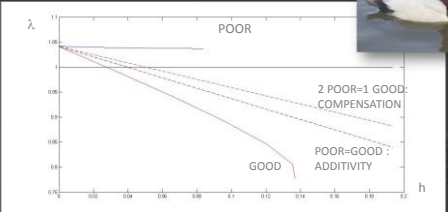



➡ “POOR” individuals more vulnerable to hunting than “GOOD”  
“Die from hunting before dying from other cause”  
Even under exchange between POOR and GOOD

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / HARVEST MANAGEMENT / CONCLUSION

### Compensation by heterogeneity: Individual Frailty

Lindberg, Lebreton, Boomer, unpublished

➡ Intimately linked with REPRODUCTIVE VALUE  
 $P1 = 0.1544$   $G1 = 1.1233$   $P2+ = 0.2233$   $G2+ = 1.1233$   
Contribution to future growth is the common currency for harvest

WATERFOWL HARVEST / WATERFOWL DEMOGRAPHY / **HARVEST MANAGEMENT** / CONCLUSION

Reproductive Value (RV) and harvest (MacArthur 1960)

**Compensation by heterogeneity**

=

**harvest of low Reproductive Value**

**Biologically significant iff RV strongly uneven**

RV(autumn) < RV(spring)  
 RV(young) < RV(adult)  
 RV(sink) < RV(source)  
 RV(ill) < RV(healthy)  
 ...

## Harvest and Heterogeneity

- Heterogeneity/variation that is readily observed (age, sex, location, etc.) can be:
  - Easily dealt with in inference and modeling
  - Exploited to maximize harvest (focus harvest on individuals of low reproductive value)
- Heterogeneity in vital rates that is not readily observed can:
  - Make inference more difficult (requires mixture distributions)
  - Lead to misinterpretations (see exercise)

## Managing Exploited Populations I

- Management focus is on how exploitation influences vital rates (rates of birth, death, movement)
- Historically: focus on manner in which hunting mortality interacts with nonhunting mortality to produce overall mortality
- Additive, independent competing risks provide a theoretical framework for this (Baranov 1918), just as they do for most disease modeling

## Managing Exploited Populations II

- Anderson-Burnham (1976) brought discussions of hunting effects into the scientific arena by defining additive and compensatory mortality hypotheses
- Mechanisms that could underlie compensation are density-dependence and heterogeneity
- But additive competing risks underlie both mechanisms

## Managing Exploited Populations III

- Density-dependence:
  - Additive mortality risks, with nonhunting risks modified by post-hunting season density
- Heterogeneity:
  - Additive mortality risks, with “compensation” effected by positively correlated vital rates (good and poor with respect to both hunting and nonhunting mortality) and resultant changing group composition

## Managing Exploited Populations IV

- Although density-dependence and heterogeneity have been discussed primarily as mechanisms underlying mortality responses, they apply to reproduction and movement as well
- Given fair knowledge of population responses to harvest, management can be based on models such as those discussed in this class

## Managing Exploited Populations

V

- But what do we do in the more typical case of process uncertainty (i.e., about how the population responds to harvest)?
- Adaptive management can use multiple process models and is a defensible approach leading to:
  - State-dependent management based on current state of knowledge (estimated system and information state)
  - Learning (changes in information state)

